

Formale Baumsprachen

Task 6 (universal algebra)

- (a) Show that the mapping sub (restricted to T_Σ) is a homomorphism. Start by giving the target algebra.
- (b) Show that the principle of proof by structural induction is correct by applying concepts from universal algebra.

Task 7 (bu-det fta)

Let $\Sigma = \{\sigma^{(2)}, \alpha^{(0)}, \beta^{(0)}\}$ and $\Delta = \{\sigma^{(2)}, \gamma^{(1)}, \alpha^{(0)}\}$ be ranked alphabets. Give deterministic bu-ta \mathcal{A}_1 , \mathcal{A}_2 , and \mathcal{A}_3 that recognize L_1 , L_2 , and L_3 , respectively, where

- (a) $L_1 = \{\xi \in T_\Sigma \mid \xi \text{ contains at least one } \alpha \text{ and one } \beta\}$,
- (b) $L_2 = \{\xi \in T_\Sigma \mid \xi \text{ contains an even number of } \alpha \text{ symbols}\}$, and
- (c) $L_3 = \{\sigma(t_1, \sigma(t_2, \dots, \sigma(t_n, \alpha) \dots)) \in T_\Delta \mid n \in \mathbb{N}, t_1, \dots, t_n \in T_{\{\gamma^{(1)}, \alpha^{(0)}\}}\}$.