

# Maschinelles Übersetzen natürlicher Sprachen

## 4. Übungsblatt

2015-11-12

### Aufgabe 1

Using the context-free grammar in Figure 1, give a leftmost derivation, and the corresponding parse tree and abstract syntax tree for the sentence “I fly to Alaska”.

$S \rightarrow NP VP$   
 $NP \rightarrow \text{Pronoun} \mid \text{Proper-Noun} \mid \text{Det Nominal}$   
 $\text{Nominal} \rightarrow \text{Noun Nominal} \mid \text{Noun}$   
 $VP \rightarrow \text{Verb} \mid \text{Verb NP} \mid \text{Verb NP PP} \mid \text{Verb PP}$   
 $PP \rightarrow \text{Preposition NP}$   
 $\text{Noun} \rightarrow \text{flight} \mid \text{breeze} \mid \text{trip} \mid \text{morning} \mid \dots$   
 $\text{Verb} \rightarrow \text{is} \mid \text{prefer} \mid \text{like} \mid \text{need} \mid \text{want} \mid \text{fly}$   
 $\text{Pronoun} \rightarrow \text{me} \mid \text{I} \mid \text{you} \mid \text{it} \mid \dots$   
 $\text{Proper-Noun} \rightarrow \text{Alaska} \mid \text{Baltimore} \mid \text{Los Angeles} \mid \text{Chicago} \mid \dots$   
 $\text{Det} \rightarrow \text{the} \mid \text{a} \mid \text{an} \mid \text{this} \mid \text{these} \mid \text{that} \mid \dots$   
 $\text{Preposition} \rightarrow \text{from} \mid \text{to} \mid \text{on} \mid \text{near} \mid \dots$

Figure 1: Productions of a context-free grammar [JM09, Figs. 9.2. and 9.3, p. 330].

### Aufgabe 2

Give a context-free grammar over the terminal alphabet  $\{(, ), [, ]\}$  which represents the well-braced strings over this alphabet (Dyck language). For example,  $([ ])[ ]$  is well-braced, while  $([ ])$  is not.

### Aufgabe 3

Let  $\Sigma$  be an alphabet and  $t \in U_{\Sigma}$ . Formally define the set of positions of  $t$ , denoted by  $\text{pos}(t)$ . A position is a sequence of integers greater or equal than one. Such a sequence describes a (partial) path through the tree starting at the root. The integers determine with which sub-tree to proceed.

Let  $p \in \text{pos}(t)$ . Formally define the label of  $t$  at  $p$ , denoted by  $t(p)$ , and the sub-tree of  $t$  at  $p$ , denoted by  $t|_p$ .

### Aufgabe 4

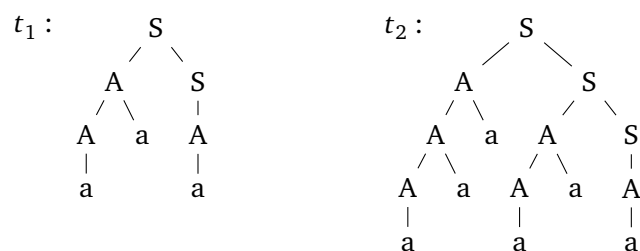
Let  $q \in [0, 1]$  and let  $(G, p)$  be a probabilistic context-free grammar with start symbol  $S$  and the following rules and probabilities:

$$\begin{aligned} S &\rightarrow SS \quad \# q \\ S &\rightarrow a \quad \# 1 - q \end{aligned}$$

1. Find (recursive) definitions for the number of derivations for  $a^n$  and the probability  $P(a^n \mid (G, p))$  where  $n \geq 1$ .
2. Show that  $(G, p)$  is consistent iff  $q \leq 0.5$ . (*Hint*: Don't get distracted by the solution of the first task.)

### Aufgabe 5

Consider the following trees.



Let  $C$  be a corpus with  $C(t_1) = 2$  and  $C(t_2) = 1$ . Train a pcfg on  $C$ .

### Aufgabe 6

Supervised training of pcfg results in proper and consistent pcfgs. Give intuitive arguments why these pcfgs are consistent.

## References

- [JM09] Daniel Jurafsky and James H. Martin. *Speech and Language Processing: An Introduction to Natural Language Processing, Computational Linguistics, and Speech Recognition*. Prentice Hall, Upper Saddle River, NJ, USA, second edition edition, 2009.