

Formale Übersetzungsmodelle

Exercise 30 (Baker's Theorem for BOT, I)

Let $\Sigma = \{\alpha^{(0)}, \gamma^{(1)}\}$, $\Delta = \{\alpha^{(0)}, \gamma^{(1)}, \sigma^{(2)}, \tau^{(2)}\}$ be ranked alphabets. Consider the bu-tt $B_1 = (Q, \Sigma, \Delta, F_1, R_1)$ and $B_2 = (P, \Delta, \Delta, F_2, R_2)$, where

- $Q = F_1 = \{*\}$, $P = \{q, p\}$, $F_2 = \{q\}$
- $R_1 = \{ \alpha \rightarrow *(\alpha), \gamma(*x_1) \rightarrow *(\sigma(x_1, x_1)), \gamma(*x_1) \rightarrow *(\tau(x_1, x_1)) \}$, and
 $R_2 = \{ \alpha \rightarrow q(\alpha), \sigma(q(x_1), q(x_2)) \rightarrow p(\sigma(x_1, x_2)), \tau(p(x_1), p(x_2)) \rightarrow q(\tau(\gamma(x_1), \gamma(x_2))) \}$.

- Do B_1 and B_2 satisfy the conditions demanded in Baker's theorem for BOT?
- Apply Baker's construction to B_1 and B_2 !
- Denote the result of the above construction by B . Is $\tau(B) = \tau(B_1) \circ \tau(B_2)$?

Exercise 31 (Baker's Theorem for BOT, II)

Let $\Sigma = \{\alpha^{(0)}, \gamma^{(1)}\}$, $\Delta = \{\alpha^{(0)}, \beta^{(0)}\}$, and $\Omega = \{\beta^{(0)}\}$ be ranked alphabets. Consider the bu-tt $B_1 = (Q, \Sigma, \Delta, F_1, R_1)$ and $B_2 = (P, \Delta, \Omega, F_2, R_2)$, where

- $Q = F_1 = \{q\}$, $P = F_2 = \{p\}$,
- $R_1 = \{ \alpha \rightarrow q(\alpha), \gamma(q(x_1)) \rightarrow q(\beta) \}$, and $R_2 = \{ \beta \rightarrow p(\beta) \}$.

- Do B_1 and B_2 satisfy the conditions demanded in Baker's theorem for BOT?
- Apply Baker's construction to B_1 and B_2 !
- Denote the result of the above construction by B . Is $\tau(B) = \tau(B_1) \circ \tau(B_2)$?

Exercise 32 (Baker's Theorem for BOT, III)

Let $\Sigma = \{\sigma^{(2)}, \tau^{(2)}, \gamma^{(1)}, \alpha^{(0)}\}$ be a ranked alphabet. Consider the bu-tt $B_1 = (Q, \Sigma, \Sigma, F_1, R_1)$ and $B_2 = (P, \Sigma, \Sigma, F_2, R_2)$, where

- $Q = F_1 = \{q\}$, $P = F_2 = \{p\}$,
- $R_1 = \{ \alpha \rightarrow q(\alpha), \gamma(q(x_1)) \rightarrow q(\sigma(x_1, x_1)) \}$, and
 $R_2 = \{ \alpha \rightarrow p(\alpha), \sigma(p(x_1), p(x_2)) \rightarrow p(\sigma(x_1, x_2)), \sigma(p(x_1), p(x_2)) \rightarrow p(\tau(x_1, x_2)) \}$.

- Do B_1 and B_2 satisfy the conditions demanded in Baker's theorem for BOT?
- Apply Baker's construction to B_1 and B_2 !
- Denote the result of the above construction by B . Is $\tau(B) = \tau(B_1) \circ \tau(B_2)$?